# $\measuredangle$ <br> <br> Computational Linguistics <br> <br> Computational Linguistics 2014-2015 

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## Practical

| Location | P0.11 (Scribanihuis) |
| :---: | :--- |
| Reading <br> material | • D. Jurafsky \& J.H. Martin (2009) Speech and Language Processing - An Introduction to Natural Language <br> Processing, Computational Linguistics, and Speech Recognition (2nd ed). Pearson Education, USA. <br> Natural Language Processing with Python |
| Software | Python 3.4 and NLTK: Installation Instructions |

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Program

| Session | Day | Date | Chapter | Topic | Reading Assignment | Slides | Take-home Assignment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Monday | 29/9/2014 | Python | Session 1 - Variables | See Github |  |  |
| 2 | Thursday | 2/10/2014 | Python | Session 2 - Collections |  |  |  |
| 3 | Monday | 6/10/2014 | Python | Session 3 - Conditions (and an introduction to loops) |  |  |  |
| 4 | Thursday | 9/10/2014 | Python | Session 4 - Loops |  |  |  |
| 5 | Monday | 13/10/2014 | Python | Session 5 - Reading and writing to files |  |  |  |
| 6 | Thursday | 16/10/2014 | Python | Session 6 - Writing your own Functions and importing packages |  |  |  |
| 7 | Monday | 20/10/2014 | Python | Session 7 - Regular Expressions in Python |  |  |  |
| 8 | Thursday | 23/10/2014 | Python | Session 8 - Advanced looping in Python and list comprehensions |  |  |  |
| 9 | Monday | 27/10/2014 | Theory | Introduction to Computational Linguistics | Jurafsky \& Martin: Chapter 1 | PDF |  |
| 10 | Monday | 3/11/2014 | Theory | Regular Expressions and Finite State Automata \& Transducers | Jurafsky \& Martin: Chapter 2; Chapter 3 | Slides morfsegment.py | See last slide. Deadline: 24/11 participles.py |
|  | Monday | 10/11/2014 | Remembrance day: no session |  |  |  |  |
| 11 | Monday | 17/11/2014 | Theory | Part-of-Speech Tagging | Jurafsky \& Martin: Chapter 5 (not 5.5, 5.8 and 5.9) | Slides <br> Python Code | See last slide. Deadline: 8/12 |
| 12 | Monday | 24/11/2014 | Theory | Syntactic Analysis \& Parsing | Jurafsky \& Martin: Chapter 12 (not 12.7.2, 12.8); Chapter 13 (not 13.4.1, 13.4.2, 13.5.1) |  |  |
| 13 | Monday | 1/12/2014 | Theory | Minimum Edit Distance + Probabilistic Methods | Jurafsky \& Martin: Chapter 3.11; Chapter 4.1, 4.2 and 4.3; Chapter 5.5 and 5.9; Chapter 14.1, 14.3 and 14.4; |  |  |
| 14 | Monday | 8/12/2014 | Theory | Word Sense Disambiguation | Jurafsky \& Martin: Chapter 19.1, 19.2, 19.3, Chapter 20 (20.1->20.5) |  |  |
| 15 | Monday | 15/12/2014 | Theory | Sentence semantics and discourse; Information extraction | Jurafsky \& Martin: Chapter 21; Chapter 22 |  |  |

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## $\measuredangle$

## Bayesian Inference

## N -gram models

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## Statistical Methods

- automatically derive statistical data from (annotated) corpora
- frequency of observed events are interpreted as the probability of those events occurring in the future
- We can use these probabilities to perform disambiguation
e.g. Most likely tag for can in "I can do this."?

$$
\mathrm{P}(\mathrm{MD} \mid c a n) \text { vs } \mathrm{P}(\mathrm{NN} \mid c a n) \text { vs } \mathrm{P}(\mathrm{VB} \mid c a n)
$$

- $\mathrm{P}(\mathrm{x} \mid \mathrm{y})$ is calculated through Bayesian Inference


## Noisy Channel

## INPUT

NOISY CHANNEL
OUTPUT

| Task | Input | Output |
| :--- | :--- | :--- |
| Speech <br> Recognition | String of Words | Acoustic Signal |
| OCR/ <br> Spellchecking | Correct Text | Text with errors |
| POS Tagging | String of POS Tags | String of words |
| Machine <br> Translation | Sentence in English | Sentence in Chinese |

## P(Input|Output) ?????

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## Bayesian Inference

Bayes' Law

$$
P(x \mid y)=\frac{P(y \mid x) \cdot P(x)}{P(y)}
$$

e.g. From Wikipedia

Drug Test: 0.99 accurate ( $99 \%$ chance that a user tests positive, $99 \%$ chance that a nonuser tests negative)
Users: $0.5 \%$ of the population
What is the probability that someone who tests positive, is a user?

$$
\begin{aligned}
\mathrm{P}(\text { User } \mid+) & =\frac{\mathrm{P}(+\mid \text { User }) . \mathrm{P}(\text { user })}{\mathrm{P}(+)} \\
& =\frac{0.99 * 0.005}{P(+\mid \text { User }) * P(\text { User })+P(+\mid \text { no }} \\
& =\frac{0.99 * 0.005}{0.99 * 0.005+0.01 * 0.995} \\
& =0.332
\end{aligned}
$$

## Bayesian Inference

Bayes' Law

$$
P(x \mid y)=\frac{P(y \mid x) \cdot P(x)}{P(y)}
$$

From a corpus we calculated the following probabilities
$\mathrm{P}($ can $\mid \mathrm{MD})=0.8$ (the frequency with which can was observed as MD)
$\mathrm{P}($ can $\mid \mathrm{NN})=0.1$ and $\mathrm{P}($ can $\mid \mathrm{VB})=0.1$
$P(M D)=0.05, P(N N)=0.3$ and $P(V B)=0.1$
$P(c a n)=0.00001$
What is $P(M D \mid c a n)$, the probability that we need to tag MD when we see 'can'?
$\begin{aligned} P(M D \mid c a n) & =\frac{P(\text { can } \mid M D) \cdot P(M D)}{P(c a n)} \\ & =\frac{0.8 * 0.05}{1}=0.04\end{aligned}$
$P(N N \mid c a n)=P($ can $\mid N N) \cdot P(N N)=0.1 * 0.3=0.03$
$P(V B \mid$ can $)=P($ can $\mid V B) \cdot P(V B)=0.1 * 0.1=0.01$

## Exercise

$P(x \mid y)=\frac{P(y \mid x) \cdot P(x)}{P(y)}$
"can" is counted 60 times as "MD" in corpusA and 40 times as "NN". In corpusB "can" is counted 70 times as "NN" and 30 times as "MD".

1. What is the probability of "can" as "MD" in corpusA?
2. What is the probability of "can" as "NN" in corpusB?
3. We pick a sentence randomly from one of the 2 corpora: "I can do this"

What is the probability that this sentence came from corpusA?

Exercise
$P(x \mid y)=\frac{P(y \mid x) \cdot P(x)}{P(y)}$
"can" is counted 60 times as "MD" in corpusA and 40 times as "NN". In corpusB "can" is counted 70 times as "NN" and 30 times as "MD".

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What is the probability that this sentence came from corpusA?

```
\(\mathrm{P}(\) corpusA|canMD) \(\quad=(\mathrm{P}(\) canMD|corpusA).P(corpusA))/ \(\mathrm{P}(\) canMD \()\)
    \(=(60 / 100 \times 1 / 2) /(60+30 / 200)\)
    \(=(0.6 \times 0.5) / 0.45\)
    \(=0.667\)
```

Bayesian Inference

In language technology, we calculate the probability of the association between an input sequence and an output sequence.
e.g. Machine translation
argmaxInput $\mathrm{P}($ fille|girl $)=$

## argmaxInput P (fille) $\quad \mathrm{P}$ (girl|fille)

Prior Likelihood
(Language
Model)
(Domain Model)

## Bayesian Inference

argmaxInput $\mathrm{P}($ fille|girl $)=$

$$
\begin{array}{c|c}
\text { argmaxInput } P(\text { fille }) & P(\text { girl|fille }) \\
\text { Prior } & \begin{array}{c}
\text { Likelihood } \\
\text { (Language } \\
\text { Model) }
\end{array} \\
\text { (Domain } \\
\text { Model) }
\end{array}
$$

The Domain Model provides the probability that girl can be translated as fille The language model provides the probability that the word fille exist (in that context)

## Bayes' Rule \& Noisy Channel

|  | P (Input) | P(Output\|Input) |
| :---: | :---: | :---: |
| Machine Translation | Language Model | Translation model |
| OCR |  | Model of OCR errors |
| Spellchecking |  | Model of spelling errors |
| POS-Tagging |  | Tag-Word Model |
| Speech Recognition |  | Acoustic model |

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## Language Model

- What is the probability of a given sequence of words, tokens, tags?
- Most common: n-gram models
- data driven: given $\quad n_{1}, n_{2}, n_{3}, n_{4}, \ldots n_{z}$
- unigram: $\quad \mathrm{P}($ word $)=$ freq (word) $/ \mathrm{N}$

$$
P(\text { sentence })=\Pi P(\text { word })
$$

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## Language Model

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$$
\mathrm{P}(\text { sentence })=\Pi \mathrm{P}(\text { word })
$$

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## Language Model

- But unigram is a weak language model
- Suppose we want to predict the most likely possible word in the sentence

Just then, the white...
According to unigram:
$P($ the $)=0.07 \quad P($ rabbit $)=0.00001$
And so
$P$ (Just then, the white the) $>P$ (Just then, the white rabbit)
Although intuitively
$P$ (Just then, the white the) $<P$ (Just then, the white rabbit)

- Contextual information limited to n-value (cfr. n-gram models)


## Language Model

- $P($ sentence $)=\Pi P($ word $)$

Unigram: $\mathrm{P}($ word $)=$ freq(word) / N bigram: $\mathrm{P}\left(\right.$ word $_{i} \mid$ word $\left._{i-1}\right)=$ freq('wordi-1 word $_{i}$ ') / freq(wordi-1)
$P($ rabbit $\mid$ white $)=$ freq $(w h i t e ~ r a b b i t) / f r e q(w h i t e) ~$
$P($ the $\mid$ white $)=$ freq(white the) $/ f$ freq(the)
data driven: given $\quad n_{1}, n_{2}, n_{3}, n_{4}, \ldots n_{z}$

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## Language Model

- $P($ sentence $)=\Pi P($ word $)$

Unigram: $\mathrm{P}($ word $)=$ freq(word) / N bigram: $\mathrm{P}\left(\right.$ word $_{i} \mid$ word $\left._{i-1}\right)=$ freq('wordi-1 word $_{i}$ ') / freq(wordi-1)
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$P($ the $\mid$ white $)=$ freq(white the)/freq(the)
data driven: given $n_{1}, n_{2}, n_{3}, n_{4}, \ldots n_{z}$

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## Language Model

- $P($ sentence $)=\Pi P($ word $)$

Unigram: $\mathrm{P}($ word $)=$ freq(word) / N bigram: $\mathrm{P}\left(\right.$ word $_{i} \mid$ word $\left._{i-1}\right)=$ freq('wordi-1 word $_{i}$ ') / freq( wordi-1 $)$
$P($ rabbit $\mid$ white $)=$ freq(white rabbit)/freq(white)
$P($ the $\mid$ white $)=$ freq(white the)/freq(the)
data driven: given

$$
\mathrm{n}_{1}, \mathrm{n}_{2}, \mathrm{n}_{3}, \mathrm{n}_{4}, \ldots \mathrm{n}_{\mathrm{z}}
$$

## Language Model

- $P($ sentence $)=\Pi P($ word $)$

Unigram: $\mathrm{P}($ word $)=$ freq(word) / N
bigram: $\mathrm{P}\left(\right.$ word $_{i} \mid$ word $\left._{i-1}\right)=$ freq('wordi-1 wordil $\left._{i}\right) /$ freq(wordi-1)
trigram: $\mathrm{P}\left(\right.$ wordil word $_{i-2}$ word $\left._{i-1}\right)=$ freq('wordi-2 $^{\text {word }_{i-1}}$ wordi' $\left._{i}\right) /$ freq( wordi-2wordi-1 $^{1}$ )
$\mathrm{P}($ rabbit|the white $)=$ freq(the white rabbit)/freq(the white)
$P($ the |the white $)=$ freq(the white the)/freq(the white)
data driven: given $\quad n_{1}, n_{2}, n_{3}, n_{4}, \ldots n_{z}$
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## Language Model

- $P($ sentence $)=\Pi P($ word $)$

Unigram: $\mathrm{P}($ word $)=$ freq(word) / N bigram: $\mathrm{P}\left(\right.$ word $_{i} \mid$ word $\left._{i-1}\right)=$ freq('wordi-1 wordil $\left._{i}\right) /$ freq( wordi-1 $)$
trigram: $\mathrm{P}\left(\right.$ wordil word $_{i-2}$ word $\left._{i-1}\right)=$ freq('word $_{i-2}$ word $_{i-1}$ wordi' $\left._{i}\right) /$ freq( wordi-2wordi-1 $^{\text {}}$ )
$\mathrm{P}($ rabbit|the white $)=$ freq(the white rabbit)/freq(the white)
$P($ the |the white $)=$ freq(the white the)/freq(the white)
data driven: given $n_{1}, n_{2}, n_{3}, n_{4}, \ldots n_{z}$
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## $\mathbf{N}$-gram models

- The higher $n$, the more context is captured
- The higher $n$, the less statistical evidence we find for each context: sparse data problem


## PCFG as a language model

$$
P(\text { tree })=\Pi P\left(\text { rule }_{\mathrm{i}}\right)
$$



16/343

$$
\begin{array}{ll}
\mathrm{P}(\text { parse }) & =\prod_{\mathrm{p}}\left(\text { rule }_{\mathrm{i}}\right) \\
\mathrm{P}(\text { sentence }) & =\Sigma \mathrm{p}\left(\text { parse }_{\mathrm{k}}\right) \\
\mathrm{P}(\text { text }) & =\Sigma \mathrm{p}\left(\text { sentence }_{\mathrm{l}}\right)
\end{array}
$$

| Bayes' Rule \&. Noisy Channel |  |  |
| :--- | :--- | :--- |
| Machine Translation |  | P(Input) |
| OCR |  | Translation model |
|  |  | Model of OCR errors |
| Spellchecking |  | Model of spelling <br> errors |
| POS-Tagging |  | Tag-Word Model |
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Probabilistic Spelling Correction

Kernighan et al (1990): misspelt word differs from correct word in 1 substition, insertion, transposition or deletion

| error | Correction | Correct <br> Letter | Error <br> Letter | Position | Type |
| :--- | :--- | :--- | :--- | :--- | :--- |
| acress | actress | t | - | 2 | deletion |
| acress | cress | - | a | 0 | insertion |
| acress | caress | ca | ac | 0 | transposition |
| acress | access | c | r | 2 | substitution |
| $\ldots$ |  |  |  |  |  |

- correction = argmaxP(t|c).P(c)
with $\mathrm{t}=$ =typo and C: list of correct words
- P(c): prior: language model (unigram)
- $P(t \mid c): \quad$ Model of misspellings

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Probabilistic Spelling Correction

- Kernighan: $44 \times 10^{6}$ word AP newswire corpus
- PRIOR:

| c | Freq(c) | $\mathrm{P}(\mathrm{c})$ |
| :--- | :--- | :--- |
| actress | 1343 | .0000315 |
| cress | 0 | .000000014 |
| caress | 4 | .0000001 |
| access | 2280 | .000058 |

Probabilistic Spelling Correction

- Kernighan: $44 \times 10^{6}$ word AP newswire corpus
- PRIOR:

| c | Freq(c) | $\mathrm{P}(\mathrm{c})$ |
| :--- | :--- | :--- |
| actress | 1343 | .0000315 |
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| caress | 4 | .0000001 |
| access | 2280 | .000058 |

smoothing

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Smoothing

What if we want to calculate the probability of something we haven't seen yet?

I like failblog

+ 'failblog' may not have been seen yet
$\rightarrow 0$ probability
$\rightarrow 0$ probability for entire sentence ( $\Pi \mathrm{P}$ (word))
- Add-1 smoothing: $\quad P($ word $)=\quad$ freq (word $)+a$

N + a.d
with a: normalization factor (often $a=1$ )
with N : total number of tokens (words)
with d: total number of types (individual words)

Probabilistic Spelling Correction

- Model of misspellings: $\mathrm{P}(\mathrm{t} \mid \mathrm{c})$
- Proper $\mathrm{P}(\mathrm{t} \mid \mathrm{c})$ cannot be computed, but can be estimated
- Use corpus of errors to construct confusion matrix of $26 \times 26$ for each type of mistake
del[ $[x, y]$ : count how many times $x y$ was typed as $x$ ins[ $x, y$ ]: count how many times $x$ was types as $x y$ sub[x,y]: count how many times $x$ was typed as $y$ trans[x,y]: how many times xy was typed as yx


## Probabilistic Spelling Correction

| Correction | $\mathbf{P}(\mathbf{c})$ | $\mathbf{P}(\mathrm{t} \\| \mathrm{c})$ | $\mathbf{p}(\mathrm{t} \\| \mathrm{c}) \mathrm{p}(\mathrm{c})$ |
| :--- | :--- | :--- | :--- |
| actress | .0000315 | .000117 | $3.69 \times 10^{-9}$ |
| cress | .000000014 | .00000144 | $2.02 \times 10^{-14}$ |
| caress | .0000001 | .0000164 | $1.64 \times 10^{-13}$ |
| access | .000058 | .000000209 | $1.21 \times 10^{-11}$ |

- acress is rewritten as 'actress'
- use more intelligent prior to improve results in context


## Bayes' Rule \& Noisy Channel

|  | P(Input) | P(Output\|Input) |
| :---: | :---: | :---: |
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## Probabilistic n-gram POS Tagging

- Requires annotated corpus
can/md the/dt tag/nn be/vb better/jjr
- Unigram: P (word|tag) $\mathrm{P}($ tag $)$
frequency of the tag for this word in corpus
- Bigram: $\quad P\left(\right.$ word $\left._{i} \mid \operatorname{tag}_{i}\right) P\left(\operatorname{tag}_{i} \mid \operatorname{tag}_{i-1}\right)$
frequency of the tag for this word in corpus, given previous tag
- Trigram: $\quad \mathrm{P}\left(\right.$ word $\left._{\mathrm{i}} \mid \operatorname{tag}_{\mathrm{i}}\right) \mathrm{P}\left(\right.$ tag $\left._{\mathrm{i}} \mid \operatorname{tag}_{\mathrm{i}-1}, \operatorname{tag}_{\mathrm{i}-2}\right)$
frequency of the tag for this word in corpus, given previous two tags
- Good Results, but possible data sparseness problems


## Bayes' Rule \& Noisy Channel

|  | P(Input) | P(Output\|Input) |
| :---: | :---: | :---: |
| Machine Translation |  | Translation model |
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## Modeling English Pronunciation Variation

- Differences in pronunciation
- 2 classes:
- allophonic variation (due to context)

$$
\begin{array}{rll}
\text { about } & - & {[\text { ax b aw }] 32 \%} \\
& - & {[\text { ax b aw t] } 16 \%} \\
& - & {[\text { ix b aw }] \quad 8 \%}
\end{array}
$$

- Lexical variation

$$
\text { about } \quad-\quad[b a w] \quad 9 \%
$$

## Modeling English Pronunciation Variation

- we can model the distribution of this variation by introducing probabilities into a FSA
= a Weighted Automaton (Markov Chain)

- Models Sociolinguistic variation

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## Modeling English Pronunciation Variation

- model allophonic variation:


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## Modeling English Pronunciation Variation

- "about": actual weighted automaton trained on pronunciations of Switchboard Corpus


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## $\measuredangle$

$$
\begin{gathered}
\text { Edit } \\
\text { Distance }
\end{gathered}
$$

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## Minimum Edit Distance

- Spell checking: check writing against list of words/morphotactics
- Suggest list of alternatives?
closest match
fuzzy match
- How to calculate the "distance" between two words: minimum edit distance
- The minimal number of deletions, insertions, substitutions to go from word $a$ to $b$

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## Minimum Edit Distance

- intention vs execution
- 3 operations (deletion, insertion, substitution)
- Alignment

| $\mathbf{i}$ | $\mathbf{n}$ | $\mathbf{t}$ | $\mathbf{e}$ | $\boldsymbol{*}$ | $\mathbf{n}$ | $\mathbf{t}$ | $\mathbf{i}$ | $\mathbf{o}$ | $\mathbf{n}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{*}$ | $\mathbf{e}$ | $\mathbf{x}$ | $\mathbf{e}$ | $\mathbf{c}$ | $\mathbf{u}$ | $\mathbf{t}$ | $\mathbf{i}$ | $\mathbf{o}$ | $\mathbf{n}$ |
| $\mathbf{d}$ | $\mathbf{s}$ | $\mathbf{s}$ |  | $\mathbf{i}$ | $\mathbf{s}$ |  |  |  |  |

- Levenshtein distance: equal weight to all operations, no substitution (1substition $=1$ deletion +1 insertion)
- Levenshtein distance of 8 in example above


## G

## Minimum Edit Distance

[delete i]
[substitute $n$ for e]
[substitute $t$ for $x$ ]
[insert c]
[substitute $n$ for u]
$i n t e n t i o n$
$n t \in n t i o n$
$e t e n t i o n$
$e x \in n t i o n$
$e x \in c n t i o n$
e $x \in c u t i o n$

## Minimum Edit Distance

- Computed through dynamic programming
- Solve problem by combining solutions to subproblems
- Table-driven
- Useful for
- Alignment
- Fuzzy string match
- Spelling correction

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Algorithm

Function LEVENSHTEIN-DISTANCE(target,source) returns levenshtein-distance
$n \leftarrow$ length(target)
$m \leftarrow$ length(source)
Create a distance matrix distance $[n+1, m+1]$
Initialize the $0^{\text {th }}$ row and column to be the distance from the empty string
distance $[0,0]=0$
for each column $i$ from 1 to $n$ do
distance $[i, 0] \leqslant$ distance $[i-1,0]+1$ (= insertion cost)
for each row $j$ from 1 to $m$ do
distance $[0, j] \leftarrow$ distance $[0, j-1]+1$ (= deletion cost)
For each column $i$ from 1 to $n$ do
for each row $j$ from 1 to $m$ do
distance $[i, j] \leftarrow$ MIN( distance $[i-1, j]+1$ (= insertion-cost),
distance $[i, j-1]+1$ (= deletion-cost),
distance $[i-1, j-1]+2$ (substition cost if $A \neq B$ )
)
Return distance[n,m]

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## Edit distance matrix

| n | 9 | 18 | $\longleftarrow \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\measuredangle \leftarrow \downarrow 12$ | $\downarrow 11$ | $\downarrow 10$ | $\downarrow 9$ | $<8$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 8 | $\downarrow 7$ | $\longleftarrow \vdash 18$ | $\longleftarrow \leftarrow 19$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\downarrow 10$ | 19 | $\measuredangle 8$ | 19 |
| i | 7 | 16 | $\longleftarrow \leftarrow 17$ | $\longleftarrow \leftarrow 18$ | $\measuredangle \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\downarrow 9$ | $\checkmark 8$ | $\leftarrow 9$ | $\leftarrow 10$ |
| t | 6 | $\downarrow 5$ | $\longleftarrow \leftarrow \downarrow 6$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow \downarrow 8$ | $\measuredangle \leftarrow \downarrow 9$ | $<8$ | $\leftarrow 9$ | $\leftarrow 10$ | $\leftarrow \downarrow 11$ |
| n | 5 | $\downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow \downarrow 6$ | $\measuredangle \leftarrow \downarrow 7$ | $\llcorner\leftarrow \downarrow 8$ | $\longleftarrow \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\longleftarrow \leftarrow \downarrow 11$ | $\checkmark \downarrow 10$ |
| e | 4 | $\checkmark 3$ | $\leftarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\leftarrow 6$ | $\leftarrow 7$ | $\longleftarrow \leftarrow \downarrow 8$ | $\measuredangle \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\downarrow 9$ |
| t | 3 | $\measuredangle \leftarrow \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\swarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow \downarrow 8$ | $\checkmark 7$ | $\leftarrow \downarrow 8$ | $\longleftarrow \vdash \downarrow 9$ | 18 |
| n | 2 | $\measuredangle \leftarrow \downarrow 3$ | $\longleftarrow \leftarrow 14$ | $\longleftarrow \leftarrow \downarrow 5$ | $\measuredangle \leftarrow 16$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \vdash 18$ | 17 | $\longleftarrow \vdash 18$ | $\checkmark 7$ |
| i | 1 | $\measuredangle \leftarrow \downarrow 2$ | $\llcorner\vdash \downarrow 3$ | $\llcorner\vdash \downarrow 4$ | $\measuredangle \leftarrow \downarrow 5$ | $\measuredangle \vdash \downarrow 6$ | $\longleftarrow \leftarrow \downarrow 7$ | $\checkmark 6$ | $\leftarrow 7$ | $\leftarrow 8$ |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|  | $\varepsilon$ | e | x | e | c | u | t | i | 0 | n |

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| n | 9 | 18 | $\measuredangle \leftarrow 19$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\measuredangle \leftarrow \downarrow 12$ | $\downarrow 11$ | $\downarrow 10$ | 19 | $\angle 8$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 8 | 17 | $\longleftarrow \leftarrow \downarrow 8$ | $\longleftarrow \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\downarrow 10$ | 19 | $\checkmark 8$ | 19 |
| i | 7 | 16 | $\longleftarrow \leftarrow 17$ | $\longleftarrow \leftarrow 18$ | $く \leftarrow 19$ | $\measuredangle \leftarrow \downarrow 10$ | $\downarrow 9$ | $\llcorner 8$ | $\leftarrow 9$ | $\leftarrow 10$ |
| t | 6 | $\downarrow 5$ | $<\leftarrow 16$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow 18$ | $\longleftarrow \leftarrow 19$ | $\angle 8$ | $\leftarrow 9$ | $\leftarrow 10$ | $\leftarrow \downarrow 11$ |
| n | 5 | 14 | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\llcorner\leftarrow \downarrow 7$ | $\llcorner\leftarrow \downarrow 8$ | $\longleftarrow \leftarrow 19$ | $\longleftarrow \vdash \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\checkmark \downarrow 10$ |
| e | 4 | $\checkmark 3$ | $\leftarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\leftarrow 6$ | $\leftarrow 7$ | $\llcorner\leftarrow 18$ | $\longleftarrow \vdash \downarrow 9$ | $\longleftarrow \leftarrow \downarrow 10$ | 19 |
| t | 3 | $\longleftarrow \leftarrow \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \vdash 16$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow 18$ | $\checkmark 7$ | $\leftarrow \downarrow 8$ | $\longleftarrow \leftarrow 19$ | 18 |
| n | 2 | $\measuredangle \leftarrow \downarrow 3$ | $\measuredangle \leftarrow 14$ | $<\leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\longleftarrow \leftarrow 17$ | $\longleftarrow \leftarrow 18$ | 17 | $\measuredangle \leftarrow 18$ | $\checkmark 7$ |
| i | 1 | $\longleftarrow \leftarrow 12$ | $\longleftarrow \leftarrow 13$ | $\longleftarrow \vdash \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\measuredangle \leftarrow 17$ | $\checkmark 6$ | $\leftarrow 7$ | $\leftarrow 8$ |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|  | $\varepsilon$ | e | x | e | c | u | t | i | 0 | n |

Edit operations are determined by starting from the top right cell, following the arrows to find a path to cello. Often, several paths are possible.

Path 1

COLO [delete i]
COL1 [substitute $n$ for e]
COL2 [substitute $t$ for $x]$
COL3
COL4 [insert c]
COL5 [substitute $n$ for u]
COL6
...COL9
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```
inten t i o n
    n t e n t i o n
    et ent i on
    e x ent i on
    ex en t i on
    ex ecn t i on
    ex e cut i o n
    e x e cut i o n
    ex e cut i o n
```

| n | 9 | 18 | $\measuredangle \leftarrow 19$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\measuredangle \leftarrow \downarrow 12$ | $\downarrow 11$ | $\downarrow 10$ | 19 | $\angle 8$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 8 | 17 | $\longleftarrow \leftarrow \downarrow 8$ | $\longleftarrow \leftarrow \downarrow 9$ | $\measuredangle \leftarrow \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\downarrow 10$ | 19 | $\checkmark 8$ | 19 |
| i | 7 | 16 | $\longleftarrow \leftarrow 17$ | $\longleftarrow \leftarrow 18$ | $く \leftarrow 19$ | $\measuredangle \leftarrow \downarrow 10$ | $\downarrow 9$ | $\llcorner 8$ | $\leftarrow 9$ | $\leftarrow 10$ |
| t | 6 | $\downarrow 5$ | $<\leftarrow 16$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow 18$ | $\longleftarrow \leftarrow 19$ | $\angle 8$ | $\leftarrow 9$ | $\leftarrow 10$ | $\leftarrow \downarrow 11$ |
| n | 5 | 14 | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow \downarrow 6$ | $\llcorner\leftarrow \downarrow 7$ | $\llcorner\leftarrow \downarrow 8$ | $\longleftarrow \leftarrow 19$ | $\longleftarrow \vdash \downarrow 10$ | $\measuredangle \leftarrow \downarrow 11$ | $\checkmark \downarrow 10$ |
| e | 4 | $\checkmark 3$ | $\leftarrow 4$ | $\longleftarrow \vdash 15$ | $\leftarrow 6$ | $\leftarrow 7$ | $\llcorner\leftarrow 18$ | $\longleftarrow \vdash \downarrow 9$ | $\longleftarrow \leftarrow \downarrow 10$ | 19 |
| t | 3 | $\longleftarrow \leftarrow \downarrow 4$ | $\longleftarrow \leftarrow 15$ | $\longleftarrow \vdash 16$ | $\longleftarrow \leftarrow \downarrow 7$ | $\longleftarrow \leftarrow 18$ | $\checkmark 7$ | $\leftarrow \downarrow 8$ | $\longleftarrow \leftarrow 19$ | 18 |
| n | 2 | $\leq \leftarrow 13$ | $<\leftarrow 14$ | $<\leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\longleftarrow \leftarrow 17$ | $\longleftarrow \leftarrow 18$ | 17 | $\measuredangle \leftarrow 18$ | $\checkmark 7$ |
| i | 1 | $\measuredangle \leftarrow \downarrow 2$ | $\measuredangle \leftarrow 13$ | $\longleftarrow \leftarrow \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\longleftarrow \leftarrow 16$ | $\measuredangle \leftarrow 17$ | $\checkmark 6$ | $\leftarrow 7$ | $\leftarrow 8$ |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|  | $\varepsilon$ | e | x | e | c | u | t | i | 0 | n |

Edit operations are determined by starting from the top right cell, following the arrows to find a path to cell0. Often, several paths are possible.

Path 1
COLOa [delete i]
COLOb [delete n]
COLOc [delete t]
COL1
COL2 [insert x]
COL3 [substitute $n$ for e]
COL4 [insert c]
COL5 [insert u]

```
inten t i o n
n t en t i o n
    t ent i on
    ention
    ention
    e x n t i o n
    e x e t i o n
    e x e c t i o n
    ex e cut i on
```


## Exercise

Calculate the levenshtein distance between
'delen' en 'gedeeld'

| $\mathbf{n}$ | 5 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{e}$ | 4 |  |  |  |  |  |  |  |
| $\mathbf{l}$ | 3 |  |  |  |  |  |  |  |
| $\mathbf{e}$ | 2 |  |  |  |  |  |  |  |
| $\mathbf{d}$ | 1 |  |  |  |  |  |  |  |
| $\mathbf{E}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{E}$ | $\mathbf{g}$ | $\mathbf{e}$ | $\mathbf{d}$ | $\mathbf{e}$ | $\mathbf{e}$ | $\mathbf{l}$ | $\mathbf{d}$ |

## Exercise

Calculate the levenshtein distance between
'delen' en `gedeeld'

| $\mathbf{n}$ | 5 | $\swarrow \leftarrow \downarrow 6$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{e}$ | 4 | $\swarrow \leftarrow \downarrow 5$ |  |  |  |  |  |  |
| $\mathbf{l}$ | 3 | $\swarrow \leftarrow \downarrow 4$ |  |  |  |  |  |  |
| $\mathbf{e}$ | 2 | $\swarrow \leftarrow \downarrow 3$ |  |  |  |  |  |  |
| $\mathbf{d}$ | 1 | $\measuredangle \leftarrow \downarrow 2$ |  |  |  |  |  |  |
| $\mathbf{E}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | $\mathbf{g}$ | $\mathbf{e}$ | $\mathbf{d}$ | $\mathbf{e}$ | $\mathbf{e}$ | $\mathbf{l}$ | $\mathbf{d}$ |

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## Exercise

Calculate the levenshtein distance between
'delen' en `gedeeld'

| $\mathbf{n}$ | 5 | $\swarrow \leftarrow \downarrow 6$ | $\downarrow 5$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{e}$ | 4 | $\swarrow \leftarrow \downarrow 5$ | $\measuredangle \downarrow 4$ |  |  |  |  |  |
| $\mathbf{l}$ | 3 | $\swarrow \leftarrow \downarrow 4$ | $\downarrow 3$ |  |  |  |  |  |
| $\mathbf{e}$ | 2 | $\swarrow \leftarrow \downarrow 3$ | $\swarrow 2$ |  |  |  |  |  |
| $\mathbf{d}$ | 1 | $\measuredangle \leftarrow \downarrow 2$ | $\measuredangle \leftarrow \downarrow 3$ |  |  |  |  |  |
| $\mathbf{E}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | $\mathbf{g}$ | $\mathbf{e}$ | $\mathbf{d}$ | $\mathbf{e}$ | $\mathbf{e}$ | $\mathbf{I}$ | $\mathbf{d}$ |

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## Exercise

Calculate the levenshtein distance between
'delen' en 'gedeeld'

| $\mathbf{n}$ | 5 | $\swarrow \leftarrow \downarrow 6$ | $\downarrow 5$ | $\swarrow \leftarrow \downarrow 6$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{e}$ | 4 | $\swarrow \leftarrow \downarrow 5$ | $\measuredangle \downarrow 4$ | $\swarrow \leftarrow \downarrow 5$ |  |  |  |  |
| $\mathbf{l}$ | 3 | $\swarrow \leftarrow \downarrow 4$ | $\downarrow 3$ | $\swarrow \leftarrow \downarrow 4$ |  |  |  |  |
| $\mathbf{e}$ | 2 | $\swarrow \leftarrow \downarrow 3$ | $\measuredangle 2$ | $\leftarrow \downarrow 3$ |  |  |  |  |
| $\mathbf{d}$ | 1 | $\measuredangle \leftarrow \downarrow 2$ | $\measuredangle \leftarrow \downarrow 3$ | $\measuredangle 2$ |  |  |  |  |
| $\mathbf{E}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | $\mathbf{g}$ | $\mathbf{e}$ | $\mathbf{d}$ | $\mathbf{e}$ | $\mathbf{e}$ | $\mathbf{l}$ | $\mathbf{d}$ |

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## Exercise

Calculate the levenshtein distance between
'delen' en `gedeeld'

| n | 5 | $\measuredangle \leftarrow \downarrow 6$ | $\downarrow 5$ | $\measuredangle \leftarrow \downarrow 6$ | $\downarrow 5$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| e | 4 | $\measuredangle \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\measuredangle \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ |  |  |  |
| I | 3 | $\measuredangle \leftarrow \downarrow 4$ | $\downarrow 3$ | $\longleftarrow \leftarrow \downarrow 4$ | $\downarrow 3$ |  |  |  |
| e | 2 | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow \downarrow 3$ | $\angle 2$ |  |  |  |
| d | 1 | $\longleftarrow \leftarrow \downarrow 2$ | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow 3$ |  |  |  |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | g | e | d | e | e | I | d |

## Exercise

Calculate the levenshtein distance between
'delen' en 'gedeeld'

| n | 5 | $\longleftarrow \leftarrow \downarrow 6$ | $\downarrow 5$ | $\measuredangle \leftarrow \downarrow 6$ | $\downarrow 5$ | $\downarrow 4$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| e | 4 | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\checkmark 3$ |  |  |
| I | 3 | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\vdash \downarrow 4$ |  |  |
| e | 2 | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow \downarrow 3$ | $\measuredangle 2$ | $\iota \leftarrow 3$ |  |  |
| d | 1 | $\longleftarrow \leftarrow \downarrow 2$ | $\llcorner\leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow 3$ | $\leftarrow 4$ |  |  |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\varepsilon$ | g | e | d | e | e | I | d |

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## Exercise

Calculate the levenshtein distance between
'delen' en `gedeeld'

| n | 5 | $\longleftarrow \leftarrow \downarrow 6$ | $\downarrow 5$ | $\measuredangle \leftarrow \downarrow 6$ | $\downarrow 5$ | $\downarrow 4$ | $\measuredangle \leftarrow \downarrow 5$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| e | 4 | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\llcorner\downarrow 4$ | $\checkmark 3$ | $\leftarrow \downarrow 4$ |  |
| I | 3 | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\vdash \downarrow 4$ | $\checkmark 3$ |  |
| e | 2 | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow \downarrow 3$ | $\measuredangle 2$ | $\measuredangle \leftarrow 3$ | $\leftarrow 4$ |  |
| d | 1 | $\longleftarrow \leftarrow \downarrow 2$ | $\llcorner\leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow 3$ | $\leftarrow 4$ | $\leftarrow 5$ |  |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | g | e | d | e | e | 1 | d |

## Exercise

Calculate the levenshtein distance between 'delen' en 'gedeeld'

| n | 5 | $\llcorner\leftarrow \downarrow 6$ | $\downarrow 5$ | $\measuredangle \leftarrow \downarrow 6$ | $\downarrow 5$ | $\downarrow 4$ | $\measuredangle \leftarrow \downarrow 5$ | $\measuredangle \leftarrow \downarrow 6$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| e | 4 | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\checkmark 3$ | $\leftarrow \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ |
| I | 3 | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\measuredangle \leftarrow \downarrow 4$ | 13 | $\llcorner\leftarrow \downarrow 4$ | $\checkmark 3$ | $\leftarrow 4$ |
| e | 2 | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow \downarrow 3$ | $\checkmark 2$ | $\measuredangle \leftarrow 3$ | $\leftarrow 4$ | $\leftarrow 5$ |
| d | 1 | $\longleftarrow \leftarrow \downarrow 2$ | $\measuredangle \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow 3$ | $\leftarrow 4$ | $\leftarrow 5$ | $\swarrow \leftarrow 6$ |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\boldsymbol{\varepsilon}$ | g | e | d | e | e | 1 | d |


| n | 5 | $\llcorner\leftarrow \downarrow 6$ | $\downarrow 5$ | $\llcorner\vdash \downarrow 6$ | $\downarrow 5$ | 14 | $\llcorner\leftarrow \downarrow 5$ | $\longleftarrow \leftarrow \downarrow 6$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| e | 4 | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ | $\checkmark \downarrow 4$ | $\checkmark 3$ | $\leftarrow \downarrow 4$ | $\longleftarrow \leftarrow \downarrow 5$ |
| I | 3 | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\leftarrow \downarrow 4$ | $\downarrow 3$ | $\llcorner\vdash \downarrow 4$ | $\checkmark 3$ | $\leftarrow 4$ |
| e | 2 | $\longleftarrow \leftarrow \downarrow 3$ | $\checkmark 2$ | $\leftarrow \downarrow 3$ | $\measuredangle 2$ | $\kappa \leftarrow 3$ | $\leftarrow 4$ | $\leftarrow 5$ |
| d | 1 | $\measuredangle \leftarrow \downarrow 2$ | $\measuredangle \leftarrow \downarrow 3$ | $\measuredangle 2$ | $\leftarrow 3$ | $\leftarrow 4$ | $\leftarrow 5$ | $\measuredangle \leftarrow 6$ |
| $\varepsilon$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|  | $\varepsilon$ | g | e | d | e | e | I | d |


| COL1 | [insert g] |
| :--- | :--- |
| COL2 | [insert e] |
| COL3 |  |
| COL4 |  |
| COL5 | [insert e] |
| COL6 |  |
| COL6b | [delete e] |
| COL7 | [substitute $n$ for $d]$ |

```
    delen
    gdel en
gedelen
gedelen
gedelen
gedeelen
gedeelen
gedeeln
gedeeld
```

Zie ook: http://www.let.rug.nl/kleiweg/lev/

Assignment
$\ggg$ from nltk.corpus import brown
>>> corpus = brown.sents()
$\ggg$ corpus[4]
[u'The', u'jury', u'said', u'it', u'did', u'find', u'that', u'many', u'of', u"Georgia's", u'registration', u'and', u'election', u'laws', u' ` ', u'are', u'outmoded', u'or', u'inadequate', u'and', u'often', u'ambiguous', u"'", u'.']

Write a script that extracts a trigram language model from this corpus. You can do this in 5 steps:

1. Create a dictionary (trigrams $=\{ \}$ ) and add all trigrams in the corpus (key) and their associated count (value).
2. Create a dictionary (bigrams $=\{ \}$ ) and add all bigrams in the corpus (key) and their associated count (value).
3. For every key in the trigram dictionary, divide the count by the value of the relevant bigram
4. Your trigram dictionary now contains probabilities
5. (save the dictionary using pickle)

Write a script that computes the probability of a sentence, according to your language model
>>> probability(corpus[4]) = <some value>
DEADLINE: 22 December 2014

Send python code through e-mail to guy.depauw@uantwerpen.be
Don't hesitate to contact your helpline guy.depauw@uantwerpen.be

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